

Name of course: Core CBCS

Scheme/Mode of Examination: CBCS Semester –III (OC)

Name of the Paper: Statistical Methods for Economics

UPC/Subject Code: 12271303 (OC)

Duration: 3 Hrs.

Maximum Marks: 75

Instructions: Answer any four questions. All questions carry equal marks. Answers may be written either in English or in Hindi but the same medium should be used throughout the paper. The use of a simple non-programmable calculator is allowed. Statistical tables are attached for your reference. In all calculations, figures should be rounded to two decimal places.

निर्देश: किन्हीं चार प्रश्नों के उत्तर दें। सभी प्रश्नों के समान अंक हैं। उत्तर अंग्रेजी या हिंदी में लिखे जा सकते हैं लेकिन पूरे पेपर में एक ही माध्यम का उपयोग किया जाना चाहिए। एक साधारण गैर-प्रोग्रामेबल कैलकुलेटर के उपयोग की अनुमति है। सांख्यिकीय टेबल आपके संदर्भ के लिए संलग्न हैं। सभी गणनाओं में, आंकड़ों को दो दशमलव स्थानों पर गोल किया जाना चाहिए।

Q1 i) Following are the scores for students of physics (X):

X	15	13	18	14.5	12	11	8.9	8
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- a) Determine the value of sample mean, sample median and 12.5% trimmed mean. Compare these values and comment on them.
 - b) A sample of three scores is drawn from the above population. How many such samples can be drawn if it is a random sample?
 - c) Suppose two such samples are (18, 12, 8)) and (13, 14.5, 11). What are the respective sample means? Is the sample mean a random variable and why?
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- ii) The current economic indicators after the pandemic indicate make forecasters think that the economy will recover from recession over the next four quarters with probability 0.4. A survey was therefore, conducted by the government to assess business intentions to expand plant and equipment. Such a survey in the past predicted a recovery when a recovery did actually occur 8 times out of 10. In 2 out of 10 cases, a recovery was predicted but it did not actually occur. In the light of this information, how might the forecaster revise his assessment of the probability that a recovery will occur?

iii) a) Rajesh wants to insure his car against theft. The value of the car is assessed at Rs 150,000/. The annual premium which he must pay to insure the car is Rs 2000. If the probability of his car being stolen is 1/10000, is his insurance contract fair?

b) Suppose a string of Diwali lights have 14 bulbs wind in series which implies that the string will work if all the bulbs work. If each bulb has a 99.9% chance of working the first time current is passed. What is the probability that the string itself will not work.

Q1 i) भौतिकी के छात्रों के लिए स्कोर निम्नलिखित हैं (X):

X	15	13	18	14.5	12	11	8.9	8
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क) नमूना औसत, नमूना माध्यिका और 12.5% छंटनी माध्य का मान निर्धारित कीजिये। इन मूल्यों की तुलना कीजिये और उन पर टिप्पणी कीजिये।

ख) तीन अंकों का एक नमूना उपरोक्त आबादी से लिया गया है। यदि नमूना यादचिक है तो ऐसे कितने नमूने खींचे जा सकते हैं?

ग) मान लीजिए कि दो ऐसे नमूने हैं (18, 12, 8) और (13, 14.5, 11)। संबंधित नमूना साधन क्या हैं? क्या नमूना एक यादचिक चर है और क्यों?

ii) महामारी का संकेत देने के बाद मौजूदा आर्थिक संकेतक यह अनुमान लगाते हैं कि अर्थव्यवस्था अगले चार तिमाहियों में मंदी से उबर जाएगी। इसलिए, सरकार द्वारा संयंत्र और उपकरणों के विस्तार के लिए व्यापारिक इरादों का आकलन करने के लिए एक सर्वेक्षण किया गया। अतीत में इस तरह के एक सर्वेक्षण ने आर्थिक पुनःप्राप्ति की भविष्यवाणी की थी जब आर्थिक पुनःप्राप्ति वास्तव में 10 में से 8 बार हुई थी। 10 में से 2 मामलों में, आर्थिक पुनःप्राप्ति की भविष्यवाणी की गई थी लेकिन यह वास्तव में नहीं हुआ था। इस जानकारी के प्रकाश में, भविष्यवक्ता इस संभावना के अपने आकलन को कैसे संशोधित कर सकता है कि आर्थिक पुनःप्राप्ति होगी?

iii) क) राजेश चोरी के खिलाफ अपनी कार का बीमा कराना चाहता है। कार का मूल्य 150,000/ रुपये आंका गया है। कार का बीमा करने के लिए उसे जो वार्षिक प्रीमियम देना होगा, वह ₹ 2000 है। यदि उसकी कार चोरी होने की संभावना 1/10000 है, तो क्या उसका बीमा अनुबंध उचित है?

ख) मान लीजिए कि दीवाली की एक स्ट्रिंग की शृंखला में 14 बल्ब की कतार होती है, जिसका अर्थ है कि यदि सभी बल्ब काम करते हैं तो स्ट्रिंग काम करेगी। यदि प्रत्येक बल्ब में 99.9% काम करने की संभावना है, तो पहली बार करंट पास होने पर क्या क्या संभावना है कि स्ट्रिंग ही काम नहीं करेगी।

- Q2 i) An inflammatory disease is a fatal genetic disease occurring mainly in children, belonging to a particular sly community. Suppose that we limit ourselves to families which have (a) exactly three children, and (b) which have both parents carrying the inflammatory disease. For such parents, the probability that a child will get the disease is 1/4. Assume each child is independent of one another. Let X be the random variable representing the number of children that will have the disease. Which distribution does X follow? What will be the pdf of X ? Find $E(X)$ and $V(X)$.
- ii) A game of Indian Premiere league of cricket is being watched in a café. It is observed that someone is clearly supporting Mumbai Indians in the game. Assume that the probability that a randomly selected person in the café is born within 25 miles of Mumbai is 1/20. The probability that a person born within 25 miles of Mumbai actually supports Mumbai Indians is 7/10 and the probability that a person not born within 25 miles of Mumbai supports Mumbai Indians is 1/10. What is the probability that the randomly selected person from the cafe was actually born within 25 miles of Mumbai?
- iii) The number of minutes Ram is early or late to work is a random variable whose pdf is given by:

$$f(x) = \begin{cases} \frac{1}{288}(36 - x^2) & \text{for } -6 < x < 6 \\ 0, & \text{elsewhere} \end{cases}$$

Where negative values are indicative of Ram being early to work and positive values are indicative of him being late for work

- a) What is the probability that one of the days he will be at least 2 minutes early to work? At least 1 minute late to work?
- b) Compute expected time taken and the standard deviation of the time taken by Ram to reach for work.
- iv) If the temperature at which ice cream melts is a random variable with mean value 120°C and standard deviation 2°C, what are the mean temperature and standard deviation in °F.? It is known that °F = 1.8°C+32

- Q2) i) एक इंफ्लेमेटरी बीमारी मुख्य रूप से बच्चों में होने वाली एक घातक आनुवंशिक बीमारी है, जो एक विशेष धूर्त समुदाय से संबंधित है। मान लीजिए कि हम खुद को उन परिवारों तक सीमित रखते हैं जिनके (ए) बिल्कुल तीन बच्चे हैं, और (बी) जिनके

माता-पिता दोनों में इंफ्लोमेटरी बीमारी है। ऐसे माता-पिता के, एक बच्चे को बीमारी होने की संभावना $1/4$ है। मान लें कि प्रत्येक बच्चा एक दूसरे से स्वतंत्र है। बता दें कि X बच्चों की संख्या का प्रतिनिधित्व करने वाला यादृच्छिक चर है जिसमें बीमारी होगी। X किस वितरण का अनुसरण करता है? X का pdf क्या होगा? $E(X)$ और $V(X)$ को ज्ञात कीजिये।

- ii) एक कैफे में भारतीय प्रीमियर लीग क्रिकेट का खेल देखा जा रहा है। यह देखा गया है कि कोई खेल में मुंबई इंडियंस का स्पष्ट समर्थन कर रहा है। मान लें कि इसकी संभावना $1/20$ है कि कैफे में एक यादृच्छिक रूप से चयनित व्यक्ति मुंबई के 25 मील के भीतर पैदा होता है। मुंबई के 25 मील के भीतर पैदा होने वाला व्यक्ति वास्तव में मुंबई इंडियंस का समर्थन करता है, इसकी संभावना $7/10$ है और मुंबई के 25 मील के भीतर पैदा नहीं होने वाला व्यक्ति मुंबई इंडियंस का समर्थन करता है इसकी संभावना $1/10$ है। क्या संभावना है कि कैफे से यादृच्छिक रूप से चयनित व्यक्ति वास्तव में मुंबई के 25 मील के भीतर पैदा हुआ था?

- iii) काम के लिए राम का जल्दी या देर से आने की संख्या एक यादृच्छिक चर है जिसका पीडीएफ (pdf) नीचे दिया गया है:

$$f(x) = \begin{cases} \frac{1}{288} (36 - x^2) & \text{for } -6 < x < 6 \\ 0, & \text{अन्यत्र} \end{cases}$$

जहाँ नकारात्मक मूल्य राम के शीघ्र काम के लिए जल्दी के संकेत देते हैं और सकारात्मक मूल्य उन्हें काम के लिए देर से आने का संकेत देते हैं

- क) क्या संभावना है कि एक दिन वह काम करने के लिए कम से कम 2 मिनट पहले आएगा? काम के लिए कम से कम 1 मिनट देर से आएगा?
- ख) काम के लिए पहुंचने के लिए राम द्वारा लिए गए अपेक्षित समय और समय के मानक विचलन की गणना कीजिये।

- iv) यदि जिस तापमान पर आइसक्रीम पिघलती है, एक यादृच्छिक चर है जिस के साथ उसका औसत मान 120°C और मानक विचलन 2°C , तो ${}^\circ\text{F}$ में औसत तापमान और मानक विचलन क्या हैं? यह ज्ञात है कि ${}^\circ\text{F} = 1.8^\circ\text{C} + 32$ ।

Q3 i) The average number of acres of land cultivated with food grains is normally distributed with mean 4,300 acres per year, and standard deviation of 750 acres. What is the probability that between 2,500 and 4,200 acres will be cultivated in any given year? What number of cultivated acres corresponds to the 38th percentile?

ii) The random variable X has a range of {0, 1, 2} and the random variable Y has a range of {1, 2}. The joint distribution of X and Y is given by the following table:

y → x ↓	1	2
0	0.2	0.1
1	0	0.2
2	0.3	0.2

- a) Find the marginal distribution of X and Y
 - b) What is the conditional distribution of X given Y=2.
 - c) Compute Cov (X,Y)
 - d) Are X and Y independent?
- iii) For short distance flights, AVX airways provides three different choices on its snack menu—mixed nuts, potato chips, and cookies. The airline observes in the past that each snack is equally likely to be chosen. If there are 150 passengers on a particular flight, what is the approximate probability that
- a) At least 60 will choose mixed nuts?
 - b) Fewer than 60 will choose mixed nuts?
- iv) Ratio of the probability of 3 successes in 5 independent trials to the probability of 2 successes in 5 independent trials is $\frac{1}{4}$. What is the probability of 4 successes in 6 independent trials?

Q3) i) खाद्यान्न के लिए खेती की गई एकड़ भूमि सामान्य रूप से वितरित हैं जिसका औसतन प्रति वर्ष 4,300 एकड़, और मानक विचलन 750 एकड़ है। क्या संभावना है कि किसी भी वर्ष में 2,500 और 4,200 एकड़ के बीच खेती की जाएगी? खेती की गई एकड़ की क्या संख्या 38 वें प्रतिशत से मेल खाती है?

ii) यादृच्छिक चर X की श्रेणी {0, 1, 2} है और यादृच्छिक चर Y की श्रेणी {1, 2} है। X और Y का संयुक्त वितरण निम्न तालिका द्वारा दिया गया है:

$y \rightarrow$ $x \downarrow$	1	2
0	0.2	0.1
1	0	0.2
2	0.3	0.2

- क) X और Y के सीमांत वितरण का ज्ञात कीजिये।
- ख) X के सशर्त वितरण का पता लगाएं यदि $Y = 2$ है।
- ग) सहप्रसरण (X, Y) $\{\text{Cov } (X, Y)\}$ का ज्ञात कीजिये।
- घ) क्या X और Y स्वतंत्र हैं?
- iii) छोटी दूरी की उड़ानों के लिए, एवीएक्स एयरवेज अपने स्नैक मेनू पर तीन अलग-अलग विकल्प प्रदान करता है- मिश्रित नट्स, आलू के चिप्स, और कुकीज़। एयरलाइन अतीत में देखती है कि प्रत्येक स्नैक को चुने जाने की समान रूप से संभावना है। यदि किसी विशेष उड़ान पर 150 यात्री हैं, तो अनुमानित संभावना क्या है कि
- क) कम से कम 60 मिश्रित नट का चयन करेंगे?
- बी) 60 से कम मिश्रित नट्स का चयन करेंगे?
- iv) 5 स्वतंत्र परीक्षणों में 3 सफलताओं को 5 स्वतंत्र परीक्षणों में 2 सफलताओं की संभावना का अनुपात $\frac{1}{4}$ है। 6 स्वतंत्र परीक्षणों में 4 सफलताओं की संभावना क्या है?

Q4 i) A particular brand of sanitiser comes in three sizes: 25 ml, 40 ml, and 65 ml. 20% of all purchasers select a 25ml bottle, 50% select 40 ml bottle and the remaining select a 65 ml bottle. Let X_1 and X_2 be the bottle sizes selected by two independently selected customers. Determine the sampling distribution of \bar{X} . Calculate $E(\bar{X})$ and compare it to μ .

- ii) a) The amount of garbage disposal by the municipality is a random variable with mean 4 tonnes and standard deviation 1.5 tonnes. If 50 trucks of garbage are independently disposed in different ways, what is the approximate probability that the sample average amount of garbage disposed is between 3.2 tonnes and 4.2 tonnes? What assumption is used here, if any?
- b) If the sample size would have been 16 instead of 50, could the probability asked in part (i) be calculated from the information provided?

- iii) A random sample of 10 tyres in a particular lot each of which is coated with durability rubber is selected and the amount of rubber (in mg) applied on them is determined. The resulting observations are 103, 156, 118, 89, 125, 147, 122, 109, 138, and 99. Let μ denote the coating of durability rubber on all the tyres. Compute a point estimate of μ .
- iv) If X and Y are independent random variables with variances $\sigma^2_X = 5$ and $\sigma^2_Y = 3$, find the variance of the random variable $Z = 2X - 4Y - 3$.

- Q4 i) सैनिटाइटर का एक विशेष ब्रांड तीन आकारों में आता है: 25 मिली, 40 मिली और 65 मिली। सभी खरीदारों में से 20%, 25ml बोतल का चयन करते हैं, 50% 40 ml की बोतल का चयन करते हैं और शेष 65 मिलीलीटर की बोतल का चयन करते हैं। बता दें कि X_1 और X_2 दो स्वतंत्र रूप से चयनित ग्राहकों द्वारा चुने गए बोतल का आकार हैं। \bar{X} का नमूना वितरण निर्धारित कीजिये। $E(\bar{X})$ की गणना कीजिये और μ से तुलना कीजिये।
- ii) क) नगरपालिका द्वारा कचरा निपटान की मात्रा एक यादृच्छिक चर है जिसका औसत 4 टन और मानक विचलन 1.5 टन है। यदि कचरे के 50 ट्रकों को अलग-अलग तरीकों से स्वतंत्र रूप से निपटाया जाता है, तो अनुमानित संभावना क्या है कि कचरे का नमूना औसत मात्रा 3.2 टन और 4.2 टन के बीच है? यदि कोई हो तो क्या धारणा यहाँ उपयोग की जाती है?
- ख) यदि नमूने का आकार 50 के बजाय 16 होगा, तो क्या भाग (i) में पूछी गई संभावना की जानकारी से गणना की जा सकती है?
- iii) एक विशेष लॉट में 10 टायरों का एक यादृच्छिक नमूना है, जिनमें से प्रत्येक को टिकाऊ रबर के साथ लेपित किया जाता है और उन पर लागू रबड़ (मिलीग्राम में) की मात्रा निर्धारित की जाती है। परिणामी अवलोकन 103, 156, 118, 89, 125, 147, 122, 109, 138, और 99 हैं। मान लीजिये कि μ सभी टायरों पर औसत टिकाऊ रबर के लेप को दर्शाता है। μ के एक बिंदु अनुमान की गणना कीजिये।
- iv) यदि X और Y स्वतंत्र रूप से भिन्न चर हैं जिनकी प्रसरण $\sigma^2_X = 5$ और $\sigma^2_Y = 3$ हैं, तो यादृच्छिक चर $Z = 2X - 4Y - 3$ का विचरण खोजिये।

- Q5 i) At a starting time $t=0$, 20 identical bulbs are tested. The lifetime distribution of each is exponential with parameter v . The experimenter then leaves the test facility unmonitored. On his return 24 hours later, the experimenter immediately terminates the

test after noticing that 15 of the 20 bulbs are still in operation (implying 5 have failed). Derive the MLE of v .

- ii) a) It was observed that aged people suffering from depression, benefit from meditation therapy. The time that they could do meditation is normally distributed with mean 65 minutes and standard deviation of 25 minutes. A new meditation video has been launched and producers of the video wish to estimate the true average time μ spent by the aged people doing meditation using the new video. A sample of 50 older people was surveyed and sample mean was found to be 57 minutes. Assuming that the time for which the aged people can still do meditation is also normally distributed, construct a 95% confidence interval for the true average time spent doing meditation.
- b) What sample size is necessary to ensure that the resulting 95% confidence interval has a width of at most 10 minutes? Without calculation, how do you think that the required sample would change if the width would be at most 12 minutes?
- iii) Out of a random sample of 500 people travelling by metro, 104 were women.
- Estimate the proportion of all travellers who are women.
 - Estimate the standard error of the estimate in part a)
 - For what value of p (the population proportion) is the standard error of its estimator maximum?
 - Construct an 89% confidence interval for the population proportion of women travellers.
 - Does the true proportion lie in the confidence interval constructed in part (d)?
- iv) If U and W are two independent standard normal random variables and $Y=0.6U+0.8W$. Determine $\text{Corr}(U,Y)$

Q5 i) शुरूआती समय $t = 0$ में, 20 समान बल्बों का परीक्षण किया जाता है। प्रत्येक का आजीवन वितरण पैरामीटर v के साथ घातांक है। प्रयोग करने वाला तब परीक्षण सुविधा को बिना अनुमति के छोड़ देता है। 24 घंटे बाद उसकी वापसी पर, प्रयोगकर्ता तुरंत परीक्षण को समाप्त करने के बाद सूचित करता है कि 20 बल्बों में से 15 अभी भी ऑपरेशन में हैं (5 असफल रहे हैं)। v के MLE व्युत्पन्न कीजिये।

ii) क) यह देखा गया कि अवसाद से पीड़ित वृद्ध लोग ध्यान चिकित्सा से लाभान्वित होते हैं। जिस समय वे ध्यान कर सकते थे, वह सामान्य रूप से वितरित किया जाता है जिसका औसतन 65 मिनट और मानक विचलन 25 मिनट है। एक नया मेडिटेशन

वीडियो लॉन्च किया गया है और वीडियो के निर्माता नए वीडियो का उपयोग करके ध्यान कर रहे वृद्धि लोगों द्वारा खर्च किए गए सही औसत समय μ का अनुमान लगाना चाहते हैं। 50 वृद्धि लोगों के नमूने का सर्वेक्षण किया गया और नमूना का औसत 57 मिनट पाया गया। यह मानते हुए कि जिस समय के लिए वृद्धि लोग अभी भी ध्यान कर सकते हैं वह भी सामान्य रूप से वितरित किया जाता है, ध्यान करने में खर्च किए गए सही औसत समय के लिए 95% आत्मविश्वास अंतराल का निर्माण कीजिये।

ख) क्या नमूना आकार यह सुनिश्चित करने के लिए आवश्यक है कि परिणामस्वरूप 95% आत्मविश्वास अंतराल की चौड़ाई अधिकतम 10 मिनट है? गणना के बिना, आपको कैसे लगता है कि आवश्यक नमूना आकार बदल जाएगा यदि अधिकतम चौड़ाई 12 की होगी?

iii) मेट्रो द्वारा यात्रा करने वाले 500 लोगों के यादचिक नमूने में से 104 महिलाएं थीं।

क) उन सभी यात्रियों के अनुपात का अनुमान लगाएं जो महिला हैं।

ख) भाग क) में अनुमान की मानक त्रुटि का अनुमान लगाएं।

ग) पी के किस मूल्य (जनसंख्या अनुपात) के लिए अपने अनुमानक की मानक त्रुटि अधिकतम है?

ड) महिला यात्रियों की जनसंख्या अनुपात के लिए 89% विश्वास अंतराल का निर्माण कीजिये।

ई) क्या भाग (ड) में निर्मित आत्मविश्वास अंतराल में सही अनुपात है?

iv) यदि U और W दो स्वतंत्र मानक सामान्य यादचिक चर हैं और $Y=0.6U+0.8W$ हैं। सहसंबंध (Corr) (U , Y) निर्धारित कीजिये।

- Q6 i) Derive method of moments and maximum-likelihood estimators for parameter μ based on a sample of size n from a Normal distribution having known variance σ^2 and unknown mean μ . Compute your estimators if the observed sample is 3, 6, 2, 0, 0, 3.
- ii) A pollution study of areas in Delhi found the following amount of PM2.5 (measured in ppm) in 5 different samples from various areas in Delhi

0.22, 0.27, 0.32, 0.33 and 0.36

Assuming that the population sampled is normal, construct a 90% confidence interval for the true mean level of PM2.5 in Delhi.

- iii) On the average, a certain computer part lasts ten years. The length of time the computer part lasts is exponentially distributed.
- What is the probability that a computer part lasts more than 7 years?
 - On the average, how long would five computer parts last if they are used one after another?
- iv) For a given sample size, can we say unequivocally that 99% confidence level is to be preferred to a 95% level? Why or why not?

Q6 i) पैरामीटर μ के लिए क्षणों की अधिकतम विधि और अधिकतम-संभावना अनुमानक की व्युत्पन्नति कीजिये जो कि आकार n के नमूने पर आधारित हैं अथवा सामान्य वितरण से लिया गया है, जिसका σ^2 ज्ञात है और माध्य अज्ञात है। अपने अनुमानकों की गणना कीजिये यदि देखा गया नमूना 3, 6, 2, 0, 0, 3 है।

- ii) दिल्ली में क्षेत्रों के प्रदूषण अध्ययन में दिल्ली के विभिन्न क्षेत्रों से 5 अलग-अलग नमूनों में पीएम 2.5 की निम्न मात्रा (पीपीएम में मापा गया) पाया गया।

0.22, 0.27, 0.32, 0.33 और 0.36

यह मानते हुए कि जनसंख्या का नमूना सामान्य है, दिल्ली में पीएम 2.5 के वास्तविक औसत स्तर के लिए 90% विश्वास अंतराल का निर्माण कीजिये।

- iii) औसतन, एक निश्चित कंप्यूटर हिस्सा दस साल तक रहता है। कंप्यूटर का हिस्सा जिस समय तक रहता है, वह चरघातांकी तरीके से वितरित होता है।
- क्या संभावना है कि एक कंप्यूटर हिस्सा 7 साल से अधिक समय तक रहता है?
 - औसतन, कंप्यूटर के पाँच भाग कितने समय तक चलेंगे यदि उनका उपयोग एक के बाद एक किया जाए?
- iv) किसी दिए गए नमूने के आकार के लिए, क्या हम स्पष्टया रूप से कह सकते हैं कि 99% आत्मविश्वास स्तर को 95% स्तर पर सर्व-प्रधान रखा जाता है? क्यों या क्यों नहीं?

Table A.1 Cumulative Binomial Probabilitiesa. $n = 5$

$$B(x; n, p) = \sum_{y=0}^x b(y; n, p)$$

		<i>p</i>														
		0.01	0.05	0.10	0.20	0.25	0.30	0.40	0.50	0.60	0.70	0.75	0.80	0.90	0.95	0.99
<i>x</i>	0	.951	.774	.590	.328	.237	.168	.078	.031	.010	.002	.001	.000	.000	.000	.000
	1	.999	.977	.919	.737	.633	.528	.337	.188	.087	.031	.016	.007	.000	.000	.000
	2	1.000	.999	.991	.942	.896	.837	.683	.500	.317	.163	.104	.058	.009	.001	.000
	3	1.000	1.000	1.000	.993	.984	.969	.913	.812	.663	.472	.367	.263	.081	.023	.001
	4	1.000	1.000	1.000	1.000	.999	.998	.990	.969	.922	.832	.763	.672	.410	.226	.049

b. $n = 10$

		<i>p</i>														
		0.01	0.05	0.10	0.20	0.25	0.30	0.40	0.50	0.60	0.70	0.75	0.80	0.90	0.95	0.99
<i>x</i>	0	.904	.599	.349	.107	.056	.028	.006	.001	.000	.000	.000	.000	.000	.000	.000
	1	.996	.914	.736	.376	.244	.149	.046	.011	.002	.000	.000	.000	.000	.000	.000
	2	1.000	.988	.930	.678	.526	.383	.167	.055	.012	.002	.000	.000	.000	.000	.000
	3	1.000	.999	.987	.879	.776	.650	.382	.172	.055	.011	.004	.001	.000	.000	.000
	4	1.000	1.000	.998	.967	.922	.850	.633	.377	.166	.047	.020	.006	.000	.000	.000
	5	1.000	1.000	1.000	.994	.980	.953	.834	.623	.367	.150	.078	.033	.002	.000	.000
	6	1.000	1.000	1.000	.999	.996	.989	.945	.828	.618	.350	.224	.121	.013	.001	.000
	7	1.000	1.000	1.000	1.000	1.000	.998	.988	.945	.833	.617	.474	.322	.070	.012	.000
	8	1.000	1.000	1.000	1.000	1.000	1.000	.998	.989	.954	.851	.756	.624	.264	.086	.004
	9	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.999	.994	.972	.944	.893	.651	.401	.096

c. $n = 15$

		<i>p</i>														
		0.01	0.05	0.10	0.20	0.25	0.30	0.40	0.50	0.60	0.70	0.75	0.80	0.90	0.95	0.99
<i>x</i>	0	.860	.463	.206	.035	.013	.005	.000	.000	.000	.000	.000	.000	.000	.000	.000
	1	.990	.829	.549	.167	.080	.035	.005	.000	.000	.000	.000	.000	.000	.000	.000
	2	1.000	.964	.816	.398	.236	.127	.027	.004	.000	.000	.000	.000	.000	.000	.000
	3	1.000	.995	.944	.648	.461	.297	.091	.018	.002	.000	.000	.000	.000	.000	.000
	4	1.000	.999	.987	.836	.686	.515	.217	.059	.009	.001	.000	.000	.000	.000	.000
	5	1.000	1.000	.998	.939	.852	.722	.403	.151	.034	.004	.001	.000	.000	.000	.000
	6	1.000	1.000	1.000	.982	.943	.869	.610	.304	.095	.015	.004	.001	.000	.000	.000
	7	1.000	1.000	1.000	.996	.983	.950	.787	.500	.213	.050	.017	.004	.000	.000	.000
	8	1.000	1.000	1.000	.999	.996	.985	.905	.696	.390	.131	.057	.018	.000	.000	.000
	9	1.000	1.000	1.000	1.000	.999	.996	.966	.849	.597	.278	.148	.061	.002	.000	.000
<i>x</i>	10	1.000	1.000	1.000	1.000	1.000	.999	.991	.941	.783	.485	.314	.164	.013	.001	.000
	11	1.000	1.000	1.000	1.000	1.000	1.000	.998	.982	.909	.703	.539	.352	.056	.005	.000
	12	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.996	.973	.873	.764	.602	.184	.036	.000
	13	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.995	.965	.920	.833	.451	.171	.010
	14	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.995	.987	.965	.794	.537	.140	

(continued)

Table A.1 Cumulative Binomial Probabilities (cont.)**d. $n = 20$**

$$B(x; n, p) = \sum_{y=0}^x b(y; n, p)$$

	<i>p</i>														
	0.01	0.05	0.10	0.20	0.25	0.30	0.40	0.50	0.60	0.70	0.75	0.80	0.90	0.95	0.99
0	.818	.358	.122	.012	.003	.001	.000	.000	.000	.000	.000	.000	.000	.000	.000
1	.983	.736	.392	.069	.024	.008	.001	.000	.000	.000	.000	.000	.000	.000	.000
2	.999	.925	.677	.206	.091	.035	.004	.000	.000	.000	.000	.000	.000	.000	.000
3	1.000	.984	.867	.411	.225	.107	.016	.001	.000	.000	.000	.000	.000	.000	.000
4	1.000	.997	.957	.630	.415	.238	.051	.006	.000	.000	.000	.000	.000	.000	.000
5	1.000	1.000	.989	.804	.617	.416	.126	.021	.002	.000	.000	.000	.000	.000	.000
6	1.000	1.000	.998	.913	.786	.608	.250	.058	.006	.000	.000	.000	.000	.000	.000
7	1.000	1.000	1.000	.968	.898	.772	.416	.132	.021	.001	.000	.000	.000	.000	.000
8	1.000	1.000	1.000	.990	.959	.887	.596	.252	.057	.005	.001	.000	.000	.000	.000
<i>x</i>	9	1.000	1.000	1.000	.997	.986	.952	.755	.412	.128	.017	.004	.001	.000	.000
10	1.000	1.000	1.000	.999	.996	.983	.872	.588	.245	.048	.014	.003	.000	.000	.000
11	1.000	1.000	1.000	1.000	.999	.995	.943	.748	.404	.113	.041	.010	.000	.000	.000
12	1.000	1.000	1.000	1.000	1.000	.999	.979	.868	.584	.228	.102	.032	.000	.000	.000
13	1.000	1.000	1.000	1.000	1.000	1.000	.994	.942	.750	.392	.214	.087	.002	.000	.000
14	1.000	1.000	1.000	1.000	1.000	1.000	.998	.979	.874	.584	.383	.196	.011	.000	.000
15	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.994	.949	.762	.585	.370	.043	.003	.000
16	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.999	.984	.893	.775	.589	.133	.016	.000
17	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.996	.965	.909	.794	.323	.075	.001
18	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.999	.992	.976	.931	.608	.264	.017
19	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.999	.997	.988	.878	.642	.182

(continued)

A-4 Appendix Tables

Table A.1 Cumulative Binomial Probabilities (cont.)

e. $n = 25$

$$B(x; n, p) = \sum_{y=0}^x b(y; n, p)$$

		<i>p</i>														
		0.01	0.05	0.10	0.20	0.25	0.30	0.40	0.50	0.60	0.70	0.75	0.80	0.90	0.95	0.99
<i>x</i>	0	.778	.277	.072	.004	.001	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
	1	.974	.642	.271	.027	.007	.002	.000	.000	.000	.000	.000	.000	.000	.000	.000
	2	.998	.873	.537	.098	.032	.009	.000	.000	.000	.000	.000	.000	.000	.000	.000
	3	1.000	.966	.764	.234	.096	.033	.002	.000	.000	.000	.000	.000	.000	.000	.000
	4	1.000	.993	.902	.421	.214	.090	.009	.000	.000	.000	.000	.000	.000	.000	.000
	5	1.000	.999	.967	.617	.378	.193	.029	.002	.000	.000	.000	.000	.000	.000	.000
	6	1.000	1.000	.991	.780	.561	.341	.074	.007	.000	.000	.000	.000	.000	.000	.000
	7	1.000	1.000	.998	.891	.727	.512	.154	.022	.001	.000	.000	.000	.000	.000	.000
	8	1.000	1.000	1.000	.953	.851	.677	.274	.054	.004	.000	.000	.000	.000	.000	.000
	9	1.000	1.000	1.000	.983	.929	.811	.425	.115	.013	.000	.000	.000	.000	.000	.000
	10	1.000	1.000	1.000	.994	.970	.902	.586	.212	.034	.002	.000	.000	.000	.000	.000
	11	1.000	1.000	1.000	.998	.980	.956	.732	.345	.078	.006	.001	.000	.000	.000	.000
	12	1.000	1.000	1.000	1.000	.997	.983	.846	.500	.154	.017	.003	.000	.000	.000	.000
	13	1.000	1.000	1.000	1.000	.999	.994	.922	.655	.268	.044	.020	.002	.000	.000	.000
	14	1.000	1.000	1.000	1.000	1.000	.998	.966	.788	.414	.098	.030	.006	.000	.000	.000
	15	1.000	1.000	1.000	1.000	1.000	1.000	.987	.885	.575	.189	.071	.017	.000	.000	.000
	16	1.000	1.000	1.000	1.000	1.000	1.000	.996	.946	.726	.323	.149	.047	.000	.000	.000
	17	1.000	1.000	1.000	1.000	1.000	1.000	.999	.978	.846	.488	.273	.109	.002	.000	.000
	18	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.993	.926	.659	.439	.220	.009	.000	.000
	19	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.998	.971	.807	.622	.383	.033	.001	.000
	20	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.991	.910	.786	.579	.098	.007	.000
	21	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.998	.967	.904	.766	.236	.034	.000
	22	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.991	.968	.902	.463	.127	.002
	23	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.998	.993	.973	.729	.358	.026
	24	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	.999	.996	.928	.723	.222

Table A.2 Cumulative Poisson Probabilities

$$F(x; \mu) = \sum_{y=0}^x \frac{e^{-\mu} \mu^y}{y!}$$

		<i>μ</i>									
		.1	.2	.3	.4	.5	.6	.7	.8	.9	.10
<i>x</i>	0	.905	.819	.741	.670	.607	.549	.497	.449	.407	.368
	1	.995	.982	.963	.938	.910	.878	.844	.809	.772	.736
	2	1.000	.999	.996	.992	.986	.977	.966	.953	.937	.920
	3		1.000	1.000	.999	.998	.997	.994	.991	.987	.981
	4			1.000	1.000	1.000	1.000	.999	.999	.998	.996
	5				1.000	1.000	1.000	1.000	1.000	1.000	.999
	6							1.000	1.000	1.000	1.000

(continued)

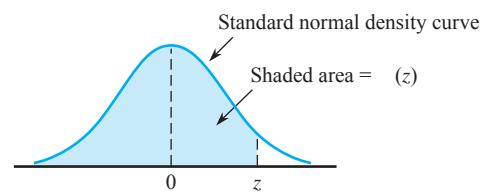
Table A.2 Cumulative Poisson Probabilities (cont.)

$$F(x; \mu) = \sum_{y=0}^x \frac{e^{-\mu} \mu^y}{y!}$$

	μ										
	2.0	3.0	4.0	5.0	6.0	7.0	8.0	9.0	10.0	15.0	20.0
0	.135	.050	.018	.007	.002	.001	.000	.000	.000	.000	.000
1	.406	.199	.092	.040	.017	.007	.003	.001	.000	.000	.000
2	.677	.423	.238	.125	.062	.030	.014	.006	.003	.000	.000
3	.857	.647	.433	.265	.151	.082	.042	.021	.010	.000	.000
4	.947	.815	.629	.440	.285	.173	.100	.055	.029	.001	.000
5	.983	.916	.785	.616	.446	.301	.191	.116	.067	.003	.000
6	.995	.966	.889	.762	.606	.450	.313	.207	.130	.008	.000
7	.999	.988	.949	.867	.744	.599	.453	.324	.220	.018	.001
8	1.000	.996	.979	.932	.847	.729	.593	.456	.333	.037	.002
9		.999	.992	.968	.916	.830	.717	.587	.458	.070	.005
10		1.000	.997	.986	.957	.901	.816	.706	.583	.118	.011
11			.999	.995	.980	.947	.888	.803	.697	.185	.021
12				1.000	.998	.991	.973	.936	.876	.792	.268
13					.999	.996	.987	.966	.926	.864	.363
14					1.000	.999	.994	.983	.959	.917	.466
15						.999	.998	.992	.978	.951	.568
16						1.000	.999	.996	.989	.973	.664
17							1.000	.998	.995	.986	.749
x	18							.999	.998	.993	.819
19								1.000	.999	.997	.875
20									1.000	.998	.917
21										.999	.947
22										1.000	.967
23											.981
24											.989
25											.994
26											.997
27											.998
28											.999
29											1.000
30											.987
31											.992
32											.995
33											.997
34											.999
35											.999
36											1.000

Table A.3 Standard Normal Curve Areas

$$(z) = P(Z \leq z)$$



<i>z</i>	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
-3.4	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0002
-3.3	.0005	.0005	.0005	.0004	.0004	.0004	.0004	.0004	.0004	.0003
-3.2	.0007	.0007	.0006	.0006	.0006	.0006	.0006	.0005	.0005	.0005
-3.1	.0010	.0009	.0009	.0009	.0008	.0008	.0008	.0008	.0007	.0007
-3.0	.0013	.0013	.0013	.0012	.0012	.0011	.0011	.0011	.0010	.0010
-2.9	.0019	.0018	.0017	.0017	.0016	.0016	.0015	.0015	.0014	.0014
-2.8	.0026	.0025	.0024	.0023	.0023	.0022	.0021	.0021	.0020	.0019
-2.7	.0035	.0034	.0033	.0032	.0031	.0030	.0029	.0028	.0027	.0026
-2.6	.0047	.0045	.0044	.0043	.0041	.0040	.0039	.0038	.0037	.0036
-2.5	.0062	.0060	.0059	.0057	.0055	.0054	.0052	.0051	.0049	.0038
-2.4	.0082	.0080	.0078	.0075	.0073	.0071	.0069	.0068	.0066	.0064
-2.3	.0107	.0104	.0102	.0099	.0096	.0094	.0091	.0089	.0087	.0084
-2.2	.0139	.0136	.0132	.0129	.0125	.0122	.0119	.0116	.0113	.0110
-2.1	.0179	.0174	.0170	.0166	.0162	.0158	.0154	.0150	.0146	.0143
-2.0	.0228	.0222	.0217	.0212	.0207	.0202	.0197	.0192	.0188	.0183
-1.9	.0287	.0281	.0274	.0268	.0262	.0256	.0250	.0244	.0239	.0233
-1.8	.0359	.0352	.0344	.0336	.0329	.0322	.0314	.0307	.0301	.0294
-1.7	.0446	.0436	.0427	.0418	.0409	.0401	.0392	.0384	.0375	.0367
-1.6	.0548	.0537	.0526	.0516	.0505	.0495	.0485	.0475	.0465	.0455
-1.5	.0668	.0655	.0643	.0630	.0618	.0606	.0594	.0582	.0571	.0559
-1.4	.0808	.0793	.0778	.0764	.0749	.0735	.0722	.0708	.0694	.0681
-1.3	.0968	.0951	.0934	.0918	.0901	.0885	.0869	.0853	.0838	.0823
-1.2	.1151	.1131	.1112	.1093	.1075	.1056	.1038	.1020	.1003	.0985
-1.1	.1357	.1335	.1314	.1292	.1271	.1251	.1230	.1210	.1190	.1170
-1.0	.1587	.1562	.1539	.1515	.1492	.1469	.1446	.1423	.1401	.1379
-0.9	.1841	.1814	.1788	.1762	.1736	.1711	.1685	.1660	.1635	.1611
-0.8	.2119	.2090	.2061	.2033	.2005	.1977	.1949	.1922	.1894	.1867
-0.7	.2420	.2389	.2358	.2327	.2296	.2266	.2236	.2206	.2177	.2148
-0.6	.2743	.2709	.2676	.2643	.2611	.2578	.2546	.2514	.2483	.2451
-0.5	.3085	.3050	.3015	.2981	.2946	.2912	.2877	.2843	.2810	.2776
-0.4	.3446	.3409	.3372	.3336	.3300	.3264	.3228	.3192	.3156	.3121
-0.3	.3821	.3783	.3745	.3707	.3669	.3632	.3594	.3557	.3520	.3482
-0.2	.4207	.4168	.4129	.4090	.4052	.4013	.3974	.3936	.3897	.3859
-0.1	.4602	.4562	.4522	.4483	.4443	.4404	.4364	.4325	.4286	.4247
-0.0	.5000	.4960	.4920	.4880	.4840	.4801	.4761	.4721	.4681	.4641

(continued)

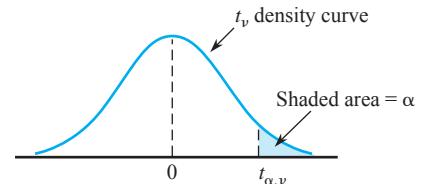
Table A.3 Standard Normal Curve Areas (cont.)

<i>z</i>	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09	$\Phi(z) = P(Z \leq z)$
0.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359	
0.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753	
0.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141	
0.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517	
0.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879	
0.5	.6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224	
0.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549	
0.7	.7580	.7611	.7642	.7673	.7704	.7734	.7764	.7794	.7823	.7852	
0.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133	
0.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389	
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621	
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8830	
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015	
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177	
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9278	.9292	.9306	.9319	
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441	
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545	
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633	
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706	
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767	
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817	
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857	
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890	
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916	
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936	
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952	
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964	
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974	
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981	
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986	
3.0	.9987	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990	
3.1	.9990	.9991	.9991	.9991	.9992	.9992	.9992	.9992	.9993	.9993	
3.2	.9993	.9993	.9994	.9994	.9994	.9994	.9994	.9995	.9995	.9995	
3.3	.9995	.9995	.9995	.9996	.9996	.9996	.9996	.9996	.9996	.9997	
3.4	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9998	

Table A.4 The Incomplete Gamma Function

$$F(x; \alpha) = \int_0^x \frac{1}{\Gamma(\alpha)} y^{\alpha-1} e^{-y} dy$$

<i>x</i> \ <i>α</i>	1	2	3	4	5	6	7	8	9	10
1	.632	.264	.080	.019	.004	.001	.000	.000	.000	.000
2	.865	.594	.323	.143	.053	.017	.005	.001	.000	.000
3	.950	.801	.577	.353	.185	.084	.034	.012	.004	.001
4	.982	.908	.762	.567	.371	.215	.111	.051	.021	.008
5	.993	.960	.875	.735	.560	.384	.238	.133	.068	.032
6	.998	.983	.938	.849	.715	.554	.394	.256	.153	.084
7	.999	.993	.970	.918	.827	.699	.550	.401	.271	.170
8	1.000	.997	.986	.958	.900	.809	.687	.547	.407	.283
9		.999	.994	.979	.945	.884	.793	.676	.544	.413
10		1.000	.997	.990	.971	.933	.870	.780	.667	.542
11			.999	.995	.985	.962	.921	.857	.768	.659
12				1.000	.998	.992	.980	.954	.911	.845
13					.999	.996	.989	.974	.946	.900
14						1.000	.998	.994	.986	.968
15							.999	.997	.992	.982
									.963	.930

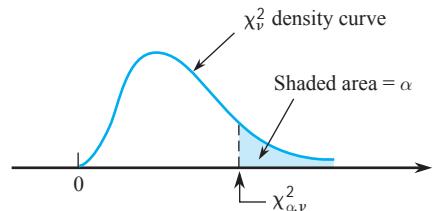
Table A.5 Critical Values for t Distributions

v	α						
	.10	.05	.025	.01	.005	.001	.0005
1	3.078	6.314	12.706	31.821	63.657	318.31	636.62
2	1.886	2.920	4.303	6.965	9.925	22.326	31.598
3	1.638	2.353	3.182	4.541	5.841	10.213	12.924
4	1.533	2.132	2.776	3.747	4.604	7.173	8.610
5	1.476	2.015	2.571	3.365	4.032	5.893	6.869
6	1.440	1.943	2.447	3.143	3.707	5.208	5.959
7	1.415	1.895	2.365	2.998	3.499	4.785	5.408
8	1.397	1.860	2.306	2.896	3.355	4.501	5.041
9	1.383	1.833	2.262	2.821	3.250	4.297	4.781
10	1.372	1.812	2.228	2.764	3.169	4.144	4.587
11	1.363	1.796	2.201	2.718	3.106	4.025	4.437
12	1.356	1.782	2.179	2.681	3.055	3.930	4.318
13	1.350	1.771	2.160	2.650	3.012	3.852	4.221
14	1.345	1.761	2.145	2.624	2.977	3.787	4.140
15	1.341	1.753	2.131	2.602	2.947	3.733	4.073
16	1.337	1.746	2.120	2.583	2.921	3.686	4.015
17	1.333	1.740	2.110	2.567	2.898	3.646	3.965
18	1.330	1.734	2.101	2.552	2.878	3.610	3.922
19	1.328	1.729	2.093	2.539	2.861	3.579	3.883
20	1.325	1.725	2.086	2.528	2.845	3.552	3.850
21	1.323	1.721	2.080	2.518	2.831	3.527	3.819
22	1.321	1.717	2.074	2.508	2.819	3.505	3.792
23	1.319	1.714	2.069	2.500	2.807	3.485	3.767
24	1.318	1.711	2.064	2.492	2.797	3.467	3.745
25	1.316	1.708	2.060	2.485	2.787	3.450	3.725
26	1.315	1.706	2.056	2.479	2.779	3.435	3.707
27	1.314	1.703	2.052	2.473	2.771	3.421	3.690
28	1.313	1.701	2.048	2.467	2.763	3.408	3.674
29	1.311	1.699	2.045	2.462	2.756	3.396	3.659
30	1.310	1.697	2.042	2.457	2.750	3.385	3.646
32	1.309	1.694	2.037	2.449	2.738	3.365	3.622
34	1.307	1.691	2.032	2.441	2.728	3.348	3.601
36	1.306	1.688	2.028	2.434	2.719	3.333	3.582
38	1.304	1.686	2.024	2.429	2.712	3.319	3.566
40	1.303	1.684	2.021	2.423	2.704	3.307	3.551
50	1.299	1.676	2.009	2.403	2.678	3.262	3.496
60	1.296	1.671	2.000	2.390	2.660	3.232	3.460
120	1.289	1.658	1.980	2.358	2.617	3.160	3.373
	1.282	1.645	1.960	2.326	2.576	3.090	3.291

Table A6 Tolerance Critical Values for Normal Population Distributions

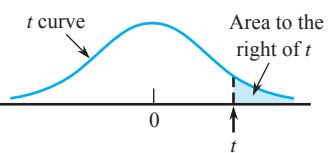
Confidence Level % of Population Captured	Two-sided Intervals					One-sided Intervals				
	95%	≥ 90%	≥ 95%	≥ 99%	99%	95%	≥ 90%	≥ 95%	99%	95%
2	32.019	37.674	48.430	160.193	188.491	242.300	20.581	26.260	37.094	103.029
3	8.380	9.916	12.861	18.930	22.401	29.055	6.156	7.656	10.553	13.995
4	5.369	6.370	8.299	9.398	11.150	14.527	4.162	5.144	7.042	7.380
5	4.275	5.079	6.634	6.612	7.855	10.260	3.407	4.203	5.741	5.362
6	3.712	4.414	5.775	5.337	6.345	8.301	3.006	3.708	5.062	4.411
7	3.369	4.007	5.248	4.613	5.488	7.187	2.756	3.400	4.642	3.859
8	3.136	3.732	4.891	4.147	4.936	6.468	2.582	3.187	4.354	3.497
9	2.967	3.532	4.631	3.822	4.550	5.966	2.454	3.031	4.143	3.241
10	2.839	3.379	4.433	3.582	4.265	5.594	2.355	2.911	3.981	3.048
11	2.737	3.259	4.277	3.397	4.045	5.308	2.275	2.815	3.852	3.556
12	2.655	3.162	4.150	3.250	3.870	5.079	2.210	2.736	3.747	2.777
13	2.587	3.081	4.044	3.130	3.727	4.893	2.155	2.671	3.659	2.677
14	2.529	3.012	3.955	3.029	3.608	4.737	2.109	2.615	3.585	2.593
15	2.480	2.954	3.878	2.945	3.507	4.605	2.068	2.566	3.520	2.522
16	2.437	2.903	3.812	2.872	3.421	4.492	2.033	2.524	3.464	2.460
17	2.400	2.858	3.754	2.808	3.345	4.393	2.002	2.486	3.414	2.405
18	2.366	2.819	3.702	2.753	3.279	4.307	1.974	2.453	3.370	2.357
19	2.337	2.784	3.656	2.703	3.221	4.230	1.949	2.423	3.331	2.314
20	2.310	2.752	3.615	2.659	3.168	4.161	1.926	2.396	3.295	2.276
25	2.208	2.631	3.457	2.494	2.972	3.904	1.838	2.292	3.158	2.129
30	2.140	2.549	3.350	2.385	2.841	3.733	1.777	2.220	3.064	2.030
35	2.090	2.490	3.272	2.306	2.748	3.611	1.732	2.167	2.995	1.957
40	2.052	2.445	3.213	2.247	2.677	3.518	1.697	2.126	2.941	1.902
45	2.021	2.408	3.165	2.200	2.621	3.444	1.669	2.092	2.898	1.857
50	1.996	2.379	3.126	2.162	2.576	3.385	1.646	2.065	2.863	1.821
60	1.958	2.333	3.066	2.103	2.506	3.293	1.609	2.022	2.807	1.764
70	1.929	2.299	3.021	2.060	2.454	3.225	1.581	1.990	2.765	1.722
80	1.907	2.272	2.986	2.026	2.414	3.173	1.559	1.965	2.733	1.688
90	1.889	2.251	2.958	1.999	2.382	3.130	1.542	1.944	2.706	1.661
100	1.874	2.233	2.934	1.977	2.355	3.096	1.527	1.927	2.684	1.639
150	1.825	2.175	2.859	1.905	2.270	2.983	1.478	1.870	2.611	1.566
200	1.798	2.143	2.816	1.865	2.222	2.921	1.450	1.837	2.570	1.524
250	1.780	2.121	2.788	1.839	2.191	2.880	1.431	1.815	2.542	1.496
300	1.767	2.106	2.767	1.820	2.169	2.850	1.417	1.800	2.522	1.476
∞	1.645	1.960	2.576	1.645	1.960	2.576	1.282	1.645	2.326	1.282

Sample Size *n*

Table A.7 Critical Values for Chi-Squared Distributions

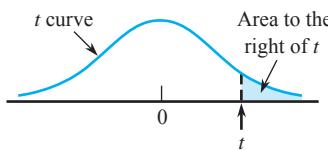
ν	α									
	.995	.99	.975	.95	.90	.10	.05	.025	.01	.005
1	0.000	0.000	0.001	0.004	0.016	2.706	3.843	5.025	6.637	7.882
2	0.010	0.020	0.051	0.103	0.211	4.605	5.992	7.378	9.210	10.597
3	0.072	0.115	0.216	0.352	0.584	6.251	7.815	9.348	11.344	12.837
4	0.207	0.297	0.484	0.711	1.064	7.779	9.488	11.143	13.277	14.860
5	0.412	0.554	0.831	1.145	1.610	9.236	11.070	12.832	15.085	16.748
6	0.676	0.872	1.237	1.635	2.204	10.645	12.592	14.440	16.812	18.548
7	0.989	1.239	1.690	2.167	2.833	12.017	14.067	16.012	18.474	20.276
8	1.344	1.646	2.180	2.733	3.490	13.362	15.507	17.534	20.090	21.954
9	1.735	2.088	2.700	3.325	4.168	14.684	16.919	19.022	21.665	23.587
10	2.156	2.558	3.247	3.940	4.865	15.987	18.307	20.483	23.209	25.188
11	2.603	3.053	3.816	4.575	5.578	17.275	19.675	21.920	24.724	26.755
12	3.074	3.571	4.404	5.226	6.304	18.549	21.026	23.337	26.217	28.300
13	3.565	4.107	5.009	5.892	7.041	19.812	22.362	24.735	27.687	29.817
14	4.075	4.660	5.629	6.571	7.790	21.064	23.685	26.119	29.141	31.319
15	4.600	5.229	6.262	7.261	8.547	22.307	24.996	27.488	30.577	32.799
16	5.142	5.812	6.908	7.962	9.312	23.542	26.296	28.845	32.000	34.267
17	5.697	6.407	7.564	8.682	10.085	24.769	27.587	30.190	33.408	35.716
18	6.265	7.015	8.231	9.390	10.865	25.989	28.869	31.526	34.805	37.156
19	6.843	7.632	8.906	10.117	11.651	27.203	30.143	32.852	36.190	38.580
20	7.434	8.260	9.591	10.851	12.443	28.412	31.410	34.170	37.566	39.997
21	8.033	8.897	10.283	11.591	13.240	29.615	32.670	35.478	38.930	41.399
22	8.643	9.542	10.982	12.338	14.042	30.813	33.924	36.781	40.289	42.796
23	9.260	10.195	11.688	13.090	14.848	32.007	35.172	38.075	41.637	44.179
24	9.886	10.856	12.401	13.848	15.659	33.196	36.415	39.364	42.980	45.558
25	10.519	11.523	13.120	14.611	16.473	34.381	37.652	40.646	44.313	46.925
26	11.160	12.198	13.844	15.379	17.292	35.563	38.885	41.923	45.642	48.290
27	11.807	12.878	14.573	16.151	18.114	36.741	40.113	43.194	46.962	49.642
28	12.461	13.565	15.308	16.928	18.939	37.916	41.337	44.461	48.278	50.993
29	13.120	14.256	16.147	17.708	19.768	39.087	42.557	45.772	49.586	52.333
30	13.787	14.954	16.791	18.493	20.599	40.256	43.773	46.979	50.892	53.672
31	14.457	15.655	17.538	19.280	21.433	41.422	44.985	48.231	52.190	55.000
32	15.134	16.362	18.291	20.072	22.271	42.585	46.194	49.480	53.486	56.328
33	15.814	17.073	19.046	20.866	23.110	43.745	47.400	50.724	54.774	57.646
34	16.501	17.789	19.806	21.664	23.952	44.903	48.602	51.966	56.061	58.964
35	17.191	18.508	20.569	22.465	24.796	46.059	49.802	53.203	57.340	60.272
36	17.887	19.233	21.336	23.269	25.643	47.212	50.998	54.437	58.619	61.581
37	18.584	19.960	22.105	24.075	26.492	48.363	52.192	55.667	59.891	62.880
38	19.289	20.691	22.878	24.884	27.343	49.513	53.384	56.896	61.162	64.181
39	19.994	21.425	23.654	25.695	28.196	50.660	54.572	58.119	62.426	65.473
40	20.706	22.164	24.433	26.509	29.050	51.805	55.758	59.342	63.691	66.766

$$\text{For } \nu > 40, \chi^2_{\alpha, \nu} \approx \nu \left(1 - \frac{2}{9\nu} + z_\alpha \sqrt{\frac{2}{9\nu}} \right)^3$$

Table A.8 t Curve Tail Areas

<i>t</i>	<i>v</i>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
0.0		.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	
0.1		.468	.465	.463	.463	.462	.462	.461	.461	.461	.461	.461	.461	.461	.461	.461	.461	.461	
0.2		.437	.430	.427	.426	.425	.424	.424	.423	.423	.423	.423	.422	.422	.422	.422	.422	.422	
0.3		.407	.396	.392	.390	.388	.387	.386	.386	.386	.385	.385	.385	.384	.384	.384	.384	.384	
0.4		.379	.364	.358	.355	.353	.352	.351	.350	.349	.349	.348	.348	.348	.347	.347	.347	.347	
0.5		.352	.333	.326	.322	.319	.317	.316	.315	.315	.314	.313	.313	.313	.312	.312	.312	.312	
0.6		.328	.305	.295	.290	.287	.285	.284	.283	.282	.281	.280	.280	.279	.279	.279	.278	.278	
0.7		.306	.278	.267	.261	.258	.255	.253	.252	.251	.250	.249	.249	.248	.247	.247	.247	.246	
0.8		.285	.254	.241	.234	.230	.227	.225	.223	.222	.221	.220	.220	.219	.218	.218	.218	.217	
0.9		.267	.232	.217	.210	.205	.201	.199	.197	.196	.195	.194	.193	.192	.191	.191	.191	.190	
1.0		.250	.211	.196	.187	.182	.178	.175	.173	.172	.170	.169	.169	.168	.167	.167	.166	.165	
1.1		.235	.193	.176	.167	.162	.157	.154	.152	.150	.149	.147	.146	.146	.144	.144	.143	.143	
1.2		.221	.177	.158	.148	.142	.138	.135	.132	.130	.129	.128	.127	.126	.124	.124	.124	.123	
1.3		.209	.162	.142	.132	.125	.121	.117	.115	.113	.111	.110	.109	.108	.107	.107	.106	.105	
1.4		.197	.148	.128	.117	.110	.106	.102	.100	.098	.096	.095	.093	.092	.091	.091	.090	.089	
1.5		.187	.136	.115	.104	.097	.092	.089	.086	.084	.082	.081	.080	.079	.077	.077	.076	.075	
1.6		.178	.125	.104	.092	.085	.080	.077	.074	.072	.070	.069	.068	.067	.065	.065	.064	.064	
1.7		.169	.116	.094	.082	.075	.070	.065	.064	.062	.060	.059	.057	.056	.055	.055	.054	.053	
1.8		.161	.107	.085	.073	.066	.061	.057	.055	.053	.051	.050	.049	.048	.046	.046	.045	.044	
1.9		.154	.099	.077	.065	.058	.053	.050	.047	.045	.043	.042	.041	.040	.038	.038	.038	.037	
2.0		.148	.092	.070	.058	.051	.046	.043	.040	.038	.037	.035	.034	.033	.032	.031	.031	.030	
2.1		.141	.085	.063	.052	.045	.040	.037	.034	.033	.031	.030	.029	.028	.027	.027	.026	.025	
2.2		.136	.079	.058	.046	.040	.035	.032	.029	.028	.026	.025	.024	.023	.022	.022	.021	.021	
2.3		.131	.074	.052	.041	.035	.031	.027	.025	.023	.022	.021	.020	.019	.018	.018	.017	.017	
2.4		.126	.069	.048	.037	.031	.027	.024	.022	.020	.019	.018	.017	.016	.015	.015	.014	.014	
2.5		.121	.065	.044	.033	.027	.023	.020	.018	.017	.016	.015	.014	.013	.012	.012	.012	.011	
2.6		.117	.061	.040	.030	.024	.020	.018	.016	.014	.013	.012	.012	.011	.010	.010	.010	.009	
2.7		.113	.057	.037	.027	.021	.018	.015	.014	.012	.011	.010	.010	.009	.008	.008	.008	.007	
2.8		.109	.054	.034	.024	.019	.016	.013	.012	.010	.009	.009	.008	.008	.007	.007	.006	.006	
2.9		.106	.051	.031	.022	.017	.014	.011	.010	.009	.008	.007	.007	.006	.005	.005	.005	.005	
3.0		.102	.048	.029	.020	.015	.012	.010	.009	.007	.007	.006	.006	.005	.004	.004	.004	.004	
3.1		.099	.045	.027	.018	.013	.011	.009	.007	.006	.006	.005	.005	.004	.004	.004	.003	.003	
3.2		.096	.043	.025	.016	.012	.009	.008	.006	.005	.005	.004	.004	.003	.003	.003	.003	.002	
3.3		.094	.040	.023	.015	.011	.008	.007	.005	.005	.004	.004	.003	.003	.002	.002	.002	.002	
3.4		.091	.038	.021	.014	.010	.007	.006	.005	.004	.003	.003	.003	.002	.002	.002	.002	.002	
3.5		.089	.036	.020	.012	.009	.006	.005	.004	.003	.003	.002	.002	.002	.002	.002	.001	.001	
3.6		.086	.035	.018	.011	.008	.006	.004	.004	.003	.002	.002	.002	.002	.001	.001	.001	.001	
3.7		.084	.033	.017	.010	.007	.005	.004	.003	.002	.002	.002	.002	.001	.001	.001	.001	.001	
3.8		.082	.031	.016	.010	.006	.004	.003	.003	.002	.002	.001	.001	.001	.001	.001	.001	.001	
3.9		.080	.030	.015	.009	.006	.004	.003	.002	.002	.001	.001	.001	.001	.001	.001	.001	.001	
4.0		.078	.029	.014	.008	.005	.004	.003	.002	.002	.001	.001	.001	.001	.001	.001	.000	.000	

(continued)

Table A.8 t Curve Tail Areas (cont.)

$t \setminus \nu$	19	20	21	22	23	24	25	26	27	28	29	30	35	40	60	120	$\infty (=z)$
0.0	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500	.500
0.1	.461	.461	.461	.461	.461	.461	.461	.461	.461	.461	.461	.461	.460	.460	.460	.460	.460
0.2	.422	.422	.422	.422	.422	.422	.422	.422	.421	.421	.421	.421	.421	.421	.421	.421	.421
0.3	.384	.384	.384	.383	.383	.383	.383	.383	.383	.383	.383	.383	.383	.383	.383	.382	.382
0.4	.347	.347	.347	.346	.346	.346	.346	.346	.346	.346	.346	.346	.346	.346	.345	.345	.345
0.5	.311	.311	.311	.311	.311	.311	.311	.311	.311	.310	.310	.310	.310	.310	.309	.309	.309
0.6	.278	.278	.278	.277	.277	.277	.277	.277	.277	.277	.277	.277	.276	.276	.275	.275	.274
0.7	.246	.246	.246	.246	.245	.245	.245	.245	.245	.245	.245	.245	.244	.244	.243	.243	.242
0.8	.217	.217	.216	.216	.216	.216	.215	.215	.215	.215	.215	.215	.215	.214	.213	.213	.212
0.9	.190	.189	.189	.189	.189	.188	.188	.188	.188	.188	.188	.188	.187	.187	.186	.185	.184
1.0	.165	.165	.164	.164	.164	.163	.163	.163	.163	.163	.163	.163	.162	.162	.161	.160	.159
1.1	.143	.142	.142	.141	.141	.141	.141	.141	.140	.140	.140	.140	.139	.139	.138	.137	.136
1.2	.122	.122	.122	.121	.121	.121	.121	.120	.120	.120	.120	.120	.119	.119	.117	.116	.115
1.3	.105	.104	.104	.104	.103	.103	.103	.103	.102	.102	.102	.102	.101	.101	.099	.098	.097
1.4	.089	.089	.088	.088	.087	.087	.087	.087	.086	.086	.086	.086	.085	.085	.083	.082	.081
1.5	.075	.075	.074	.074	.074	.073	.073	.073	.073	.072	.072	.072	.071	.071	.069	.068	.067
1.6	.063	.063	.062	.062	.062	.061	.061	.061	.061	.060	.060	.060	.059	.059	.057	.056	.055
1.7	.053	.052	.052	.052	.051	.051	.051	.051	.050	.050	.050	.050	.049	.048	.047	.046	.045
1.8	.044	.043	.043	.043	.042	.042	.042	.042	.041	.041	.041	.041	.040	.040	.038	.037	.036
1.9	.036	.036	.036	.035	.035	.035	.035	.034	.034	.034	.034	.034	.033	.032	.031	.030	.029
2.0	.030	.030	.029	.029	.029	.028	.028	.028	.028	.027	.027	.027	.026	.025	.024	.023	
2.1	.025	.024	.024	.023	.023	.023	.023	.023	.022	.022	.022	.022	.021	.020	.019	.018	
2.2	.020	.020	.020	.019	.019	.019	.018	.018	.018	.018	.018	.018	.017	.017	.016	.015	.014
2.3	.016	.016	.016	.016	.015	.015	.015	.015	.015	.014	.014	.014	.014	.013	.012	.012	.011
2.4	.013	.013	.013	.013	.012	.012	.012	.012	.012	.012	.011	.011	.011	.010	.009	.008	.008
2.5	.011	.011	.010	.010	.010	.010	.010	.009	.009	.009	.009	.009	.009	.008	.008	.007	.006
2.6	.009	.009	.008	.008	.008	.008	.008	.008	.007	.007	.007	.007	.007	.007	.006	.005	.005
2.7	.007	.007	.007	.007	.006	.006	.006	.006	.006	.006	.006	.006	.005	.005	.004	.004	.003
2.8	.006	.006	.005	.005	.005	.005	.005	.005	.005	.005	.004	.004	.004	.004	.003	.003	.003
2.9	.005	.004	.004	.004	.004	.004	.004	.004	.004	.004	.004	.003	.003	.003	.003	.002	.002
3.0	.004	.004	.003	.003	.003	.003	.003	.003	.003	.003	.003	.003	.002	.002	.002	.002	.001
3.1	.003	.003	.003	.003	.002	.002	.002	.002	.002	.002	.002	.002	.002	.002	.001	.001	.001
3.2	.002	.002	.002	.002	.002	.002	.002	.002	.002	.002	.002	.001	.001	.001	.001	.001	.001
3.3	.002	.002	.002	.002	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.000
3.4	.002	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.000	.000
3.5	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.000	.000	.000
3.6	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.001	.000	.000	.000	.000	.000
3.7	.001	.001	.001	.001	.001	.001	.001	.001	.000	.000	.000	.000	.000	.000	.000	.000	.000
3.8	.001	.001	.001	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
3.9	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
4.0	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

Table A.9 Critical Values for F Distributions

		$\nu_1 = \text{numerator df}$									
		α	1	2	3	4	5	6	7	8	9
1	.100	39.86	49.50	53.59	55.83	57.24	58.20	58.91	59.44	59.86	
	.050	161.45	199.50	215.71	224.58	230.16	233.99	236.77	238.88	240.54	
	.010	4052.20	4999.50	5403.40	5624.60	5763.60	5859.00	5928.40	5981.10	6022.50	
	.001	405,284	500,000	540,379	562,500	576,405	585,937	592,873	598,144	602,284	
2	.100	8.53	9.00	9.16	9.24	9.29	9.33	9.35	9.37	9.38	
	.050	18.51	19.00	19.16	19.25	19.30	19.33	19.35	19.37	19.38	
	.010	98.50	99.00	99.17	99.25	99.30	99.33	99.36	99.37	99.39	
	.001	998.50	999.00	999.17	999.25	999.30	999.33	999.36	999.37	999.39	
3	.100	5.54	5.46	5.39	5.34	5.31	5.28	5.27	5.25	5.24	
	.050	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81	
	.010	34.12	30.82	29.46	28.71	28.24	27.91	27.67	27.49	27.35	
	.001	167.03	148.50	141.11	137.10	134.58	132.85	131.58	130.62	129.86	
4	.100	4.54	4.32	4.19	4.11	4.05	4.01	3.98	3.95	3.94	
	.050	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00	
	.010	21.20	18.00	16.69	15.98	15.52	15.21	14.98	14.80	14.66	
	.001	74.14	61.25	56.18	53.44	51.71	50.53	49.66	49.00	48.47	
5	.100	4.06	3.78	3.62	3.52	3.45	3.40	3.37	3.34	3.32	
	.050	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77	
	.010	16.26	13.27	12.06	11.39	10.97	10.67	10.46	10.29	10.16	
	.001	47.18	37.12	33.20	31.09	29.75	28.83	28.16	27.65	27.24	
$\nu_2 = \text{denominator df}$.100	3.78	3.46	3.29	3.18	3.11	3.05	3.01	2.98	2.96	
	.050	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	
	.010	13.75	10.92	9.78	9.15	8.75	8.47	8.26	8.10	7.98	
	.001	35.51	27.00	23.70	21.92	20.80	20.03	19.46	19.03	18.69	
6	.100	3.59	3.26	3.07	2.96	2.88	2.83	2.78	2.75	2.72	
	.050	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	
	.010	12.25	9.55	8.45	7.85	7.46	7.19	6.99	6.84	6.72	
	.001	29.25	21.69	18.77	17.20	16.21	15.52	15.02	14.63	14.33	
7	.100	3.46	3.11	2.92	2.81	2.73	2.67	2.62	2.59	2.56	
	.050	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39	
	.010	11.26	8.65	7.59	7.01	6.63	6.37	6.18	6.03	5.91	
	.001	25.41	18.49	15.83	14.39	13.48	12.86	12.40	12.05	11.77	
8	.100	3.36	3.01	2.81	2.69	2.61	2.55	2.51	2.47	2.44	
	.050	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	
	.010	10.56	8.02	6.99	6.42	6.06	5.80	5.61	5.47	5.35	
	.001	22.86	16.39	13.90	12.56	11.71	11.13	10.70	10.37	10.11	
9	.100	3.29	2.92	2.73	2.61	2.52	2.46	2.41	2.38	2.35	
	.050	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	
	.010	10.04	7.56	6.55	5.99	5.64	5.39	5.20	5.06	4.94	
	.001	21.04	14.91	12.55	11.28	10.48	9.93	9.52	9.20	8.96	
10	.100	3.23	2.86	2.66	2.54	2.45	2.39	2.34	2.30	2.27	
	.050	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	
	.010	9.65	7.21	6.22	5.67	5.32	5.07	4.89	4.74	4.63	
	.001	19.69	13.81	11.56	10.35	9.58	9.05	8.66	8.35	8.12	
11	.100	3.18	2.81	2.61	2.48	2.39	2.33	2.28	2.24	2.21	
	.050	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80	
	.010	9.33	6.93	5.95	5.41	5.06	4.82	4.64	4.50	4.39	
	.001	18.64	12.97	10.80	9.63	8.89	8.38	8.00	7.71	7.48	

(continued)

Table A.9 Critical Values for F Distributions (cont.)

$\nu_1 = \text{numerator df}$										
10	12	15	20	25	30	40	50	60	120	1000
60.19	60.71	61.22	61.74	62.05	62.26	62.53	62.69	62.79	63.06	63.30
241.88	243.91	245.95	248.01	249.26	250.10	251.14	251.77	252.20	253.25	254.19
6055.80	6106.30	6157.30	6208.70	6239.80	6260.60	6286.80	6302.50	6313.00	6339.40	6362.70
605,621	610,668	615,764	620,908	624,017	626,099	628,712	630,285	631,337	633,972	636,301
9.39	9.41	9.42	9.44	9.45	9.46	9.47	9.47	9.47	9.48	9.49
19.40	19.41	19.43	19.45	19.46	19.46	19.47	19.48	19.48	19.49	19.49
99.40	99.42	99.43	99.45	99.46	99.47	99.47	99.48	99.48	99.49	99.50
999.40	999.42	999.43	999.45	999.46	999.47	999.47	999.48	999.48	999.49	999.50
5.23	5.22	5.20	5.18	5.17	5.17	5.16	5.15	5.15	5.14	5.13
8.79	8.74	8.70	8.66	8.63	8.62	8.59	8.58	8.57	8.55	8.53
27.23	27.05	26.87	26.69	26.58	26.50	26.41	26.35	26.32	26.22	26.14
129.25	128.32	127.37	126.42	125.84	125.45	124.96	124.66	124.47	123.97	123.53
3.92	3.90	3.87	3.84	3.83	3.82	3.80	3.80	3.79	3.78	3.76
5.96	5.91	5.86	5.80	5.77	5.75	5.72	5.70	5.69	5.66	5.63
14.55	14.37	14.20	14.02	13.91	13.84	13.75	13.69	13.65	13.56	13.47
48.05	47.41	46.76	46.10	45.70	45.43	45.09	44.88	44.75	44.40	44.09
3.30	3.27	3.24	3.21	3.19	3.17	3.16	3.15	3.14	3.12	3.11
4.74	4.68	4.62	4.56	4.52	4.50	4.46	4.44	4.43	4.40	4.37
10.05	9.89	9.72	9.55	9.45	9.38	9.29	9.24	9.20	9.11	9.03
26.92	26.42	25.91	25.39	25.08	24.87	24.60	24.44	24.33	24.06	23.82
2.94	2.90	2.87	2.84	2.81	2.80	2.78	2.77	2.76	2.74	2.72
4.06	4.00	3.94	3.87	3.83	3.81	3.77	3.75	3.74	3.70	3.67
7.87	7.72	7.56	7.40	7.30	7.23	7.14	7.09	7.06	6.97	6.89
18.41	17.99	17.56	17.12	16.85	16.67	16.44	16.31	16.21	15.98	15.77
2.70	2.67	2.63	2.59	2.57	2.56	2.54	2.52	2.51	2.49	2.47
3.64	3.57	3.51	3.44	3.40	3.38	3.34	3.32	3.30	3.27	3.23
6.62	6.47	6.31	6.16	6.06	5.99	5.91	5.86	5.82	5.74	5.66
14.08	13.71	13.32	12.93	12.69	12.53	12.33	12.20	12.12	11.91	11.72
2.54	2.50	2.46	2.42	2.40	2.38	2.36	2.35	2.34	2.32	2.30
3.35	3.28	3.22	3.15	3.11	3.08	3.04	3.02	3.01	2.97	2.93
5.81	5.67	5.52	5.36	5.26	5.20	5.12	5.07	5.03	4.95	4.87
11.54	11.19	10.84	10.48	10.26	10.11	9.92	9.80	9.73	9.53	9.36
2.42	2.38	2.34	2.30	2.27	2.25	2.23	2.22	2.21	2.18	2.16
3.14	3.07	3.01	2.94	2.89	2.86	2.83	2.80	2.79	2.75	2.71
5.26	5.11	4.96	4.81	4.71	4.65	4.57	4.52	4.48	4.40	4.32
9.89	9.57	9.24	8.90	8.69	8.55	8.37	8.26	8.19	8.00	7.84
2.32	2.28	2.24	2.20	2.17	2.16	2.13	2.12	2.11	2.08	2.06
2.98	2.91	2.85	2.77	2.73	2.70	2.66	2.64	2.62	2.58	2.54
4.85	4.71	4.56	4.41	4.31	4.25	4.17	4.12	4.08	4.00	3.92
8.75	8.45	8.13	7.80	7.60	7.47	7.30	7.19	7.12	6.94	6.78
2.25	2.21	2.17	2.12	2.10	2.08	2.05	2.04	2.03	2.00	1.98
2.85	2.79	2.72	2.65	2.60	2.57	2.53	2.51	2.49	2.45	2.41
4.54	4.40	4.25	4.10	4.01	3.94	3.86	3.81	3.78	3.69	3.61
7.92	7.63	7.32	7.01	6.81	6.68	6.52	6.42	6.35	6.18	6.02
2.19	2.15	2.10	2.06	2.03	2.01	1.99	1.97	1.96	1.93	1.91
2.75	2.69	2.62	2.54	2.50	2.47	2.43	2.40	2.38	2.34	2.30
4.30	4.16	4.01	3.86	3.76	3.70	3.62	3.57	3.54	3.45	3.37
7.29	7.00	6.71	6.40	6.22	6.09	5.93	5.83	5.76	5.59	5.44

(continued)

Table A.9 Critical Values for F Distributions (cont.)

		$\nu_1 = \text{numerator df}$									
		α	1	2	3	4	5	6	7	8	9
13	.100	3.14	2.76	2.56	2.43	2.35	2.28	2.23	2.20	2.16	
	.050	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71	
	.010	9.07	6.70	5.74	5.21	4.86	4.62	4.44	4.30	4.19	
	.001	17.82	12.31	10.21	9.07	8.35	7.86	7.49	7.21	6.98	
14	.100	3.10	2.73	2.52	2.39	2.31	2.24	2.19	2.15	2.12	
	.050	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65	
	.010	8.86	6.51	5.56	5.04	4.69	4.46	4.28	4.14	4.03	
	.001	17.14	11.78	9.73	8.62	7.92	7.44	7.08	6.80	6.58	
15	.100	3.07	2.70	2.49	2.36	2.27	2.21	2.16	2.12	2.09	
	.050	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59	
	.010	8.68	6.36	5.42	4.89	4.56	4.32	4.14	4.00	3.89	
	.001	16.59	11.34	9.34	8.25	7.57	7.09	6.74	6.47	6.26	
16	.100	3.05	2.67	2.46	2.33	2.24	2.18	2.13	2.09	2.06	
	.050	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54	
	.010	8.53	6.23	5.29	4.77	4.44	4.20	4.03	3.89	3.78	
	.001	16.12	10.97	9.01	7.94	7.27	6.80	6.46	6.19	5.98	
17	.100	3.03	2.64	2.44	2.31	2.22	2.15	2.10	2.06	2.03	
	.050	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49	
	.010	8.40	6.11	5.19	4.67	4.34	4.10	3.93	3.79	3.68	
	.001	15.72	10.66	8.73	7.68	7.02	6.56	6.22	5.96	5.75	
18	.100	3.01	2.62	2.42	2.29	2.20	2.13	2.08	2.04	2.00	
	.050	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46	
	.010	8.29	6.01	5.09	4.58	4.25	4.01	3.84	3.71	3.60	
	.001	15.38	10.39	8.49	7.46	6.81	6.35	6.02	5.76	5.56	
19	.100	2.99	2.61	2.40	2.27	2.18	2.11	2.06	2.02	1.98	
	.050	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42	
	.010	8.18	5.93	5.01	4.50	4.17	3.94	3.77	3.63	3.52	
	.001	15.08	10.16	8.28	7.27	6.62	6.18	5.85	5.59	5.39	
20	.100	2.97	2.59	2.38	2.25	2.16	2.09	2.04	2.00	1.96	
	.050	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39	
	.010	8.10	5.85	4.94	4.43	4.10	3.87	3.70	3.56	3.46	
	.001	14.82	9.95	8.10	7.10	6.46	6.02	5.69	5.44	5.24	
21	.100	2.96	2.57	2.36	2.23	2.14	2.08	2.02	1.98	1.95	
	.050	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37	
	.010	8.02	5.78	4.87	4.37	4.04	3.81	3.64	3.51	3.40	
	.001	14.59	9.77	7.94	6.95	6.32	5.88	5.56	5.31	5.11	
22	.100	2.95	2.56	2.35	2.22	2.13	2.06	2.01	1.97	1.93	
	.050	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34	
	.010	7.95	5.72	4.82	4.31	3.99	3.76	3.59	3.45	3.35	
	.001	14.38	9.61	7.80	6.81	6.19	5.76	5.44	5.19	4.99	
23	.100	2.94	2.55	2.34	2.21	2.11	2.05	1.99	1.95	1.92	
	.050	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32	
	.010	7.88	5.66	4.76	4.26	3.94	3.71	3.54	3.41	3.30	
	.001	14.20	9.47	7.67	6.70	6.08	5.65	5.33	5.09	4.89	
24	.100	2.93	2.54	2.33	2.19	2.10	2.04	1.98	1.94	1.91	
	.050	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30	
	.010	7.82	5.61	4.72	4.22	3.90	3.67	3.50	3.36	3.26	
	.001	14.03	9.34	7.55	6.59	5.98	5.55	5.23	4.99	4.80	

(continued)

Table A.9 Critical Values for F Distributions (cont.)

$\nu_1 = \text{numerator df}$										
10	12	15	20	25	30	40	50	60	120	1000
2.14	2.10	2.05	2.01	1.98	1.96	1.93	1.92	1.90	1.88	1.85
2.67	2.60	2.53	2.46	2.41	2.38	2.34	2.31	2.30	2.25	2.21
4.10	3.96	3.82	3.66	3.57	3.51	3.43	3.38	3.34	3.25	3.18
6.80	6.52	6.23	5.93	5.75	5.63	5.47	5.37	5.30	5.14	4.99
2.10	2.05	2.01	1.96	1.93	1.91	1.89	1.87	1.86	1.83	1.80
2.60	2.53	2.46	2.39	2.34	2.31	2.27	2.24	2.22	2.18	2.14
3.94	3.80	3.66	3.51	3.41	3.35	3.27	3.22	3.18	3.09	3.02
6.40	6.13	5.85	5.56	5.38	5.25	5.10	5.00	4.94	4.77	4.62
2.06	2.02	1.97	1.92	1.89	1.87	1.85	1.83	1.82	1.79	1.76
2.54	2.48	2.40	2.33	2.28	2.25	2.20	2.18	2.16	2.11	2.07
3.80	3.67	3.52	3.37	3.28	3.21	3.13	3.08	3.05	2.96	2.88
6.08	5.81	5.54	5.25	5.07	4.95	4.80	4.70	4.64	4.47	4.33
2.03	1.99	1.94	1.89	1.86	1.84	1.81	1.79	1.78	1.75	1.72
2.49	2.42	2.35	2.28	2.23	2.19	2.15	2.12	2.11	2.06	2.02
3.69	3.55	3.41	3.26	3.16	3.10	3.02	2.97	2.93	2.84	2.76
5.81	5.55	5.27	4.99	4.82	4.70	4.54	4.45	4.39	4.23	4.08
2.00	1.96	1.91	1.86	1.83	1.81	1.78	1.76	1.75	1.72	1.69
2.45	2.38	2.31	2.23	2.18	2.15	2.10	2.08	2.06	2.01	1.97
3.59	3.46	3.31	3.16	3.07	3.00	2.92	2.87	2.83	2.75	2.66
5.58	5.32	5.05	4.78	4.60	4.48	4.33	4.24	4.18	4.02	3.87
1.98	1.93	1.89	1.84	1.80	1.78	1.75	1.74	1.72	1.69	1.66
2.41	2.34	2.27	2.19	2.14	2.11	2.06	2.04	2.02	1.97	1.92
3.51	3.37	3.23	3.08	2.98	2.92	2.84	2.78	2.75	2.66	2.58
5.39	5.13	4.87	4.59	4.42	4.30	4.15	4.06	4.00	3.84	3.69
1.96	1.91	1.86	1.81	1.78	1.76	1.73	1.71	1.70	1.67	1.64
2.38	2.31	2.23	2.16	2.11	2.07	2.03	2.00	1.98	1.93	1.88
3.43	3.30	3.15	3.00	2.91	2.84	2.76	2.71	2.67	2.58	2.50
5.22	4.97	4.70	4.43	4.26	4.14	3.99	3.90	3.84	3.68	3.53
1.94	1.89	1.84	1.79	1.76	1.74	1.71	1.69	1.68	1.64	1.61
2.35	2.28	2.20	2.12	2.07	2.04	1.99	1.97	1.95	1.90	1.85
3.37	3.23	3.09	2.94	2.84	2.78	2.69	2.64	2.61	2.52	2.43
5.08	4.82	4.56	4.29	4.12	4.00	3.86	3.77	3.70	3.54	3.40
1.92	1.87	1.83	1.78	1.74	1.72	1.69	1.67	1.66	1.62	1.59
2.32	2.25	2.18	2.10	2.05	2.01	1.96	1.94	1.92	1.87	1.82
3.31	3.17	3.03	2.88	2.79	2.72	2.64	2.58	2.55	2.46	2.37
4.95	4.70	4.44	4.17	4.00	3.88	3.74	3.64	3.58	3.42	3.28
1.90	1.86	1.81	1.76	1.73	1.70	1.67	1.65	1.64	1.60	1.57
2.30	2.23	2.15	2.07	2.02	1.98	1.94	1.91	1.89	1.84	1.79
3.26	3.12	2.98	2.83	2.73	2.67	2.58	2.53	2.50	2.40	2.32
4.83	4.58	4.33	4.06	3.89	3.78	3.63	3.54	3.48	3.32	3.17
1.89	1.84	1.80	1.74	1.71	1.69	1.66	1.64	1.62	1.59	1.55
2.27	2.20	2.13	2.05	2.00	1.96	1.91	1.88	1.86	1.81	1.76
3.21	3.07	2.93	2.78	2.69	2.62	2.54	2.48	2.45	2.35	2.27
4.73	4.48	4.23	3.96	3.79	3.68	3.53	3.44	3.38	3.22	3.08
1.88	1.83	1.78	1.73	1.70	1.67	1.64	1.62	1.61	1.57	1.54
2.25	2.18	2.11	2.03	1.97	1.94	1.89	1.86	1.84	1.79	1.74
3.17	3.03	2.89	2.74	2.64	2.58	2.49	2.44	2.40	2.31	2.22
4.64	4.39	4.14	3.87	3.71	3.59	3.45	3.36	3.29	3.14	2.99

(continued)

Table A.9 Critical Values for F Distributions (cont.)

		$\nu_1 = \text{numerator df}$								
		1	2	3	4	5	6	7	8	9
$\nu_2 = \text{denominator df}$.100	2.92	2.53	2.32	2.18	2.09	2.02	1.97	1.93	1.89
	.050	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.28
	.010	7.77	5.57	4.68	4.18	3.85	3.63	3.46	3.32	3.22
	.001	13.88	9.22	7.45	6.49	5.89	5.46	5.15	4.91	4.71
	.100	2.91	2.52	2.31	2.17	2.08	2.01	1.96	1.92	1.88
	.050	4.23	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.27
	.010	7.72	5.53	4.64	4.14	3.82	3.59	3.42	3.29	3.18
	.001	13.74	9.12	7.36	6.41	5.80	5.38	5.07	4.83	4.64
	.100	2.90	2.51	2.30	2.17	2.07	2.00	1.95	1.91	1.87
	.050	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.25
27	.010	7.68	5.49	4.60	4.11	3.78	3.56	3.39	3.26	3.15
	.001	13.61	9.02	7.27	6.33	5.73	5.31	5.00	4.76	4.57
	.100	2.89	2.50	2.29	2.16	2.06	2.00	1.94	1.90	1.87
	.050	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.24
	.010	7.64	5.45	4.57	4.07	3.75	3.53	3.36	3.23	3.12
	.001	13.50	8.93	7.19	6.25	5.66	5.24	4.93	4.69	4.50
	.100	2.89	2.50	2.28	2.15	2.06	1.99	1.93	1.89	1.86
	.050	4.18	3.33	2.93	2.70	2.55	2.43	2.35	2.28	2.22
	.010	7.60	5.42	4.54	4.04	3.73	3.50	3.33	3.20	3.09
	.001	13.39	8.85	7.12	6.19	5.59	5.18	4.87	4.64	4.45
30	.100	2.88	2.49	2.28	2.14	2.05	1.98	1.93	1.88	1.85
	.050	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21
	.010	7.56	5.39	4.51	4.02	3.70	3.47	3.30	3.17	3.07
	.001	13.29	8.77	7.05	6.12	5.53	5.12	4.82	4.58	4.39
	.100	2.84	2.44	2.23	2.09	2.00	1.93	1.87	1.83	1.79
	.050	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12
	.010	7.31	5.18	4.31	3.83	3.51	3.29	3.12	2.99	2.89
	.001	12.61	8.25	6.59	5.70	5.13	4.73	4.44	4.21	4.02
	.100	2.81	2.41	2.20	2.06	1.97	1.90	1.84	1.80	1.76
	.050	4.03	3.18	2.79	2.56	2.40	2.29	2.20	2.13	2.07
50	.010	7.17	5.06	4.20	3.72	3.41	3.19	3.02	2.89	2.78
	.001	12.22	7.96	6.34	5.46	4.90	4.51	4.22	4.00	3.82
	.100	2.79	2.39	2.18	2.04	1.95	1.87	1.82	1.77	1.74
	.050	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04
	.010	7.08	4.98	4.13	3.65	3.34	3.12	2.95	2.82	2.72
	.001	11.97	7.77	6.17	5.31	4.76	4.37	4.09	3.86	3.69
	.100	2.76	2.36	2.14	2.00	1.91	1.83	1.78	1.73	1.69
	.050	3.94	3.09	2.70	2.46	2.31	2.19	2.10	2.03	1.97
	.010	6.90	4.82	3.98	3.51	3.21	2.99	2.82	2.69	2.59
	.001	11.50	7.41	5.86	5.02	4.48	4.11	3.83	3.61	3.44
200	.100	2.73	2.33	2.11	1.97	1.88	1.80	1.75	1.70	1.66
	.050	3.89	3.04	2.65	2.42	2.26	2.14	2.06	1.98	1.93
	.010	6.76	4.71	3.88	3.41	3.11	2.89	2.73	2.60	2.50
	.001	11.15	7.15	5.63	4.81	4.29	3.92	3.65	3.43	3.26
	.100	2.71	2.31	2.09	1.95	1.85	1.78	1.72	1.68	1.64
	.050	3.85	3.00	2.61	2.38	2.22	2.11	2.02	1.95	1.89
	.010	6.66	4.63	3.80	3.34	3.04	2.82	2.66	2.53	2.43
	.001	10.89	6.96	5.46	4.65	4.14	3.78	3.51	3.30	3.13

(continued)

Table A.9 Critical Values for F Distributions (cont.)

$\nu_1 = \text{numerator df}$										
10	12	15	20	25	30	40	50	60	120	1000
1.87	1.82	1.77	1.72	1.68	1.66	1.63	1.61	1.59	1.56	1.52
2.24	2.16	2.09	2.01	1.96	1.92	1.87	1.84	1.82	1.77	1.72
3.13	2.99	2.85	2.70	2.60	2.54	2.45	2.40	2.36	2.27	2.18
4.56	4.31	4.06	3.79	3.63	3.52	3.37	3.28	3.22	3.06	2.91
1.86	1.81	1.76	1.71	1.67	1.65	1.61	1.59	1.58	1.54	1.51
2.22	2.15	2.07	1.99	1.94	1.90	1.85	1.82	1.80	1.75	1.70
3.09	2.96	2.81	2.66	2.57	2.50	2.42	2.36	2.33	2.23	2.14
4.48	4.24	3.99	3.72	3.56	3.44	3.30	3.21	3.15	2.99	2.84
1.85	1.80	1.75	1.70	1.66	1.64	1.60	1.58	1.57	1.53	1.50
2.20	2.13	2.06	1.97	1.92	1.88	1.84	1.81	1.79	1.73	1.68
3.06	2.93	2.78	2.63	2.54	2.47	2.38	2.33	2.29	2.20	2.11
4.41	4.17	3.92	3.66	3.49	3.38	3.23	3.14	3.08	2.92	2.78
1.84	1.79	1.74	1.69	1.65	1.63	1.59	1.57	1.56	1.52	1.48
2.19	2.12	2.04	1.96	1.91	1.87	1.82	1.79	1.77	1.71	1.66
3.03	2.90	2.75	2.60	2.51	2.44	2.35	2.30	2.26	2.17	2.08
4.35	4.11	3.86	3.60	3.43	3.32	3.18	3.09	3.02	2.86	2.72
1.83	1.78	1.73	1.68	1.64	1.62	1.58	1.56	1.55	1.51	1.47
2.18	2.10	2.03	1.94	1.89	1.85	1.81	1.77	1.75	1.70	1.65
3.00	2.87	2.73	2.57	2.48	2.41	2.33	2.27	2.23	2.14	2.05
4.29	4.05	3.80	3.54	3.38	3.27	3.12	3.03	2.97	2.81	2.66
1.82	1.77	1.72	1.67	1.63	1.61	1.57	1.55	1.54	1.50	1.46
2.16	2.09	2.01	1.93	1.88	1.84	1.79	1.76	1.74	1.68	1.63
2.98	2.84	2.70	2.55	2.45	2.39	2.30	2.25	2.21	2.11	2.02
4.24	4.00	3.75	3.49	3.33	3.22	3.07	2.98	2.92	2.76	2.61
1.76	1.71	1.66	1.61	1.57	1.54	1.51	1.48	1.47	1.42	1.38
2.08	2.00	1.92	1.84	1.78	1.74	1.69	1.66	1.64	1.58	1.52
2.80	2.66	2.52	2.37	2.27	2.20	2.11	2.06	2.02	1.92	1.82
3.87	3.64	3.40	3.14	2.98	2.87	2.73	2.64	2.57	2.41	2.25
1.73	1.68	1.63	1.57	1.53	1.50	1.46	1.44	1.42	1.38	1.33
2.03	1.95	1.87	1.78	1.73	1.69	1.63	1.60	1.58	1.51	1.45
2.70	2.56	2.42	2.27	2.17	2.10	2.01	1.95	1.91	1.80	1.70
3.67	3.44	3.20	2.95	2.79	2.68	2.53	2.44	2.38	2.21	2.05
1.71	1.66	1.60	1.54	1.50	1.48	1.44	1.41	1.40	1.35	1.30
1.99	1.92	1.84	1.75	1.69	1.65	1.59	1.56	1.53	1.47	1.40
2.63	2.50	2.35	2.20	2.10	2.03	1.94	1.88	1.84	1.73	1.62
3.54	3.32	3.08	2.83	2.67	2.55	2.41	2.32	2.25	2.08	1.92
1.66	1.61	1.56	1.49	1.45	1.42	1.38	1.35	1.34	1.28	1.22
1.93	1.85	1.77	1.68	1.62	1.57	1.52	1.48	1.45	1.38	1.30
2.50	2.37	2.22	2.07	1.97	1.89	1.80	1.74	1.69	1.57	1.45
3.30	3.07	2.84	2.59	2.43	2.32	2.17	2.08	2.01	1.83	1.64
1.63	1.58	1.52	1.46	1.41	1.38	1.34	1.31	1.29	1.23	1.16
1.88	1.80	1.72	1.62	1.56	1.52	1.46	1.41	1.39	1.30	1.21
2.41	2.27	2.13	1.97	1.87	1.79	1.69	1.63	1.58	1.45	1.30
3.12	2.90	2.67	2.42	2.26	2.15	2.00	1.90	1.83	1.64	1.43
1.61	1.55	1.49	1.43	1.38	1.35	1.30	1.27	1.25	1.18	1.08
1.84	1.76	1.68	1.58	1.52	1.47	1.41	1.36	1.33	1.24	1.11
2.34	2.20	2.06	1.90	1.79	1.72	1.61	1.54	1.50	1.35	1.16
2.99	2.77	2.54	2.30	2.14	2.02	1.87	1.77	1.69	1.49	1.22